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New numerical approaches to model hydraulic fracturing in tight reservoirs with consideration of hydro-mechanical coupling effects

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**New numerical approaches to
model hydraulic fracturing in
tight reservoirs with
consideration of hydro-
mechanical coupling effects**

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