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**Robustness Concepts for Knapsack and Network
Design Problems under Data Uncertainty**
Gamma-, Multi-band, Submodular, and Recoverable
Robustness

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