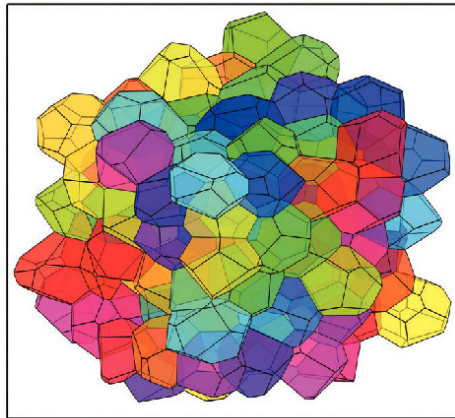




Luis Antonio Barrales Mora (Autor)
2D and 3D Grain Growth Modeling and Simulation

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and Simulation

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