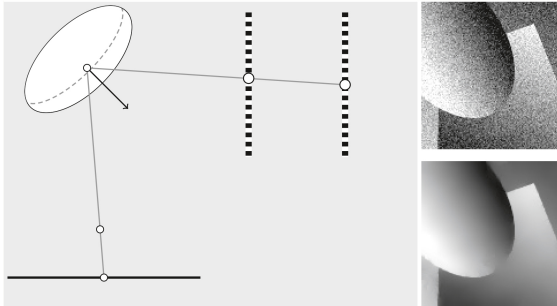




Birgit Komander (Autor)  
**Deflectometry and Image Denoising**



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Image Denoising**

Birgit Komander



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